

# PID Tuning for Temperature Control of Heated Plates Using the Waterbed Effect

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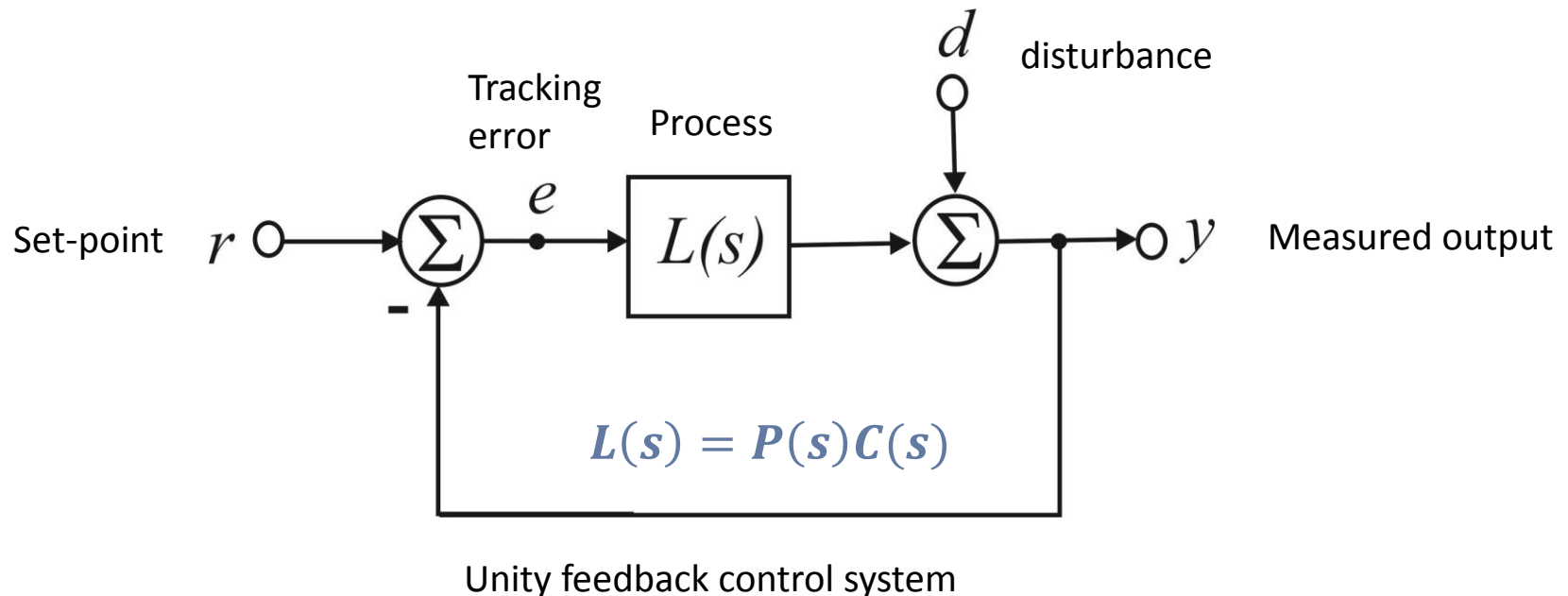
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- ❑ **The Waterbed Effect Theory**
- ❑ Using the Theory for PID Tuning
- ❑ Application to a Heated Plate
- ❑ Summary & Conclusions

# The Waterbed Effect

- ❑ There is a fundamental and inescapable limitation on achievable design specifications in feedback control systems
- ❑ The sensitivity function,  $|S(s)|$  is the transfer function from the reference input  $r$  (Set-point) to the tracking error  $e$
- ❑ The overall transfer function gain is less sensitive to variations in the process gain by a factor of  $|S|$

$$E(s) = (I + L(s))^{-1} R(s) = S(s)R(s)$$



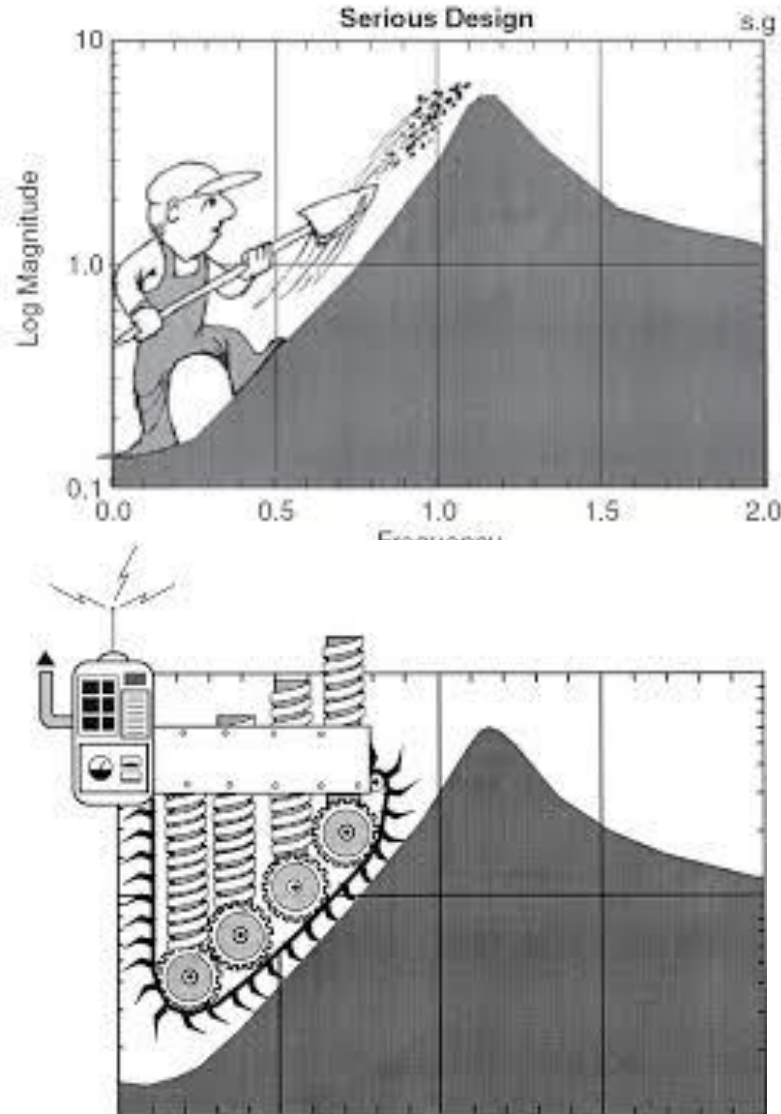
# The Waterbed Effect

- Bode showed that for a system with an excess of at least two more poles than zeros and no right-half plane (RHP) poles,  $\int_0^{\infty} \ln(|S|) d\omega = 0$
- This means that if the sensitivity is to be reduced in a certain frequency range, then of it must be increased in another frequency range. This is referred to as the waterbed effect.
- If the system has  $n_p$  unstable poles then,  $\int_0^{\infty} \ln(|S|) d\omega = \sum_{i=1}^{n_p} \text{Re}\{p_i\}$
- Recently [Emami-Naeini, D. de Roover, 2015] we have derived a new fundamental result that has been seemingly masked by previous derivations :

$$\int_0^{\infty} \ln |s(j\omega)| d\omega = \begin{cases} -\frac{\pi}{2} \left( \sum_{i=1}^n (\tilde{p}_i - p_i) \right), OLS \\ -\frac{\pi}{2} \left( \sum_{i=1}^n (\tilde{p}_i - p_i) + \sum_{i=1}^{n_p} 2p_i \right), OLU \end{cases}$$

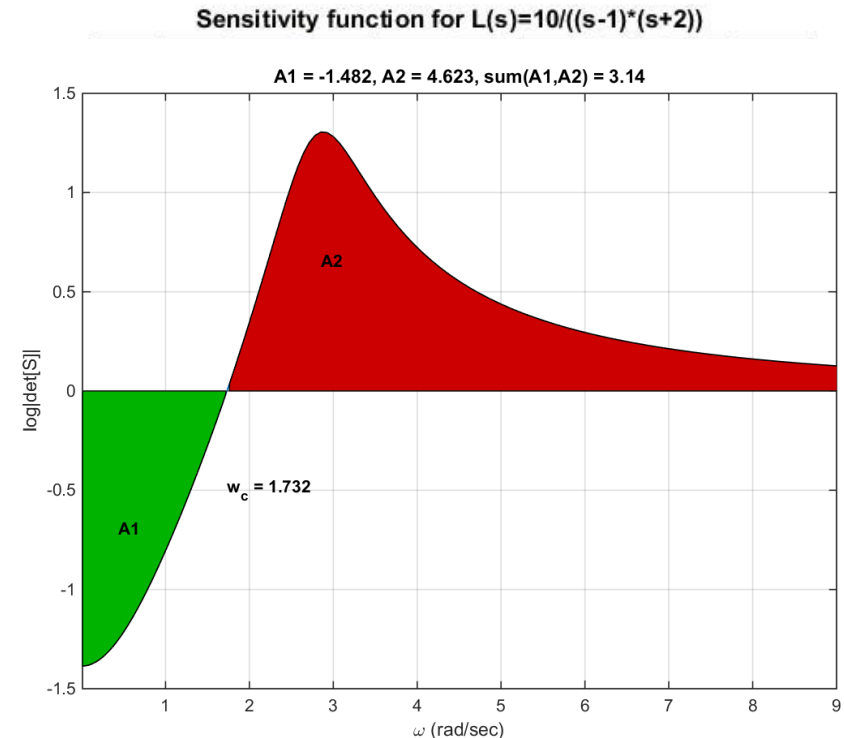
- The fundamental relationship is that the sum of **areas** underneath the  $\ln(|S|)$  is related to the **difference** in speeds of the closed-loop system and the open-loop system. This makes much intuitive sense.

# The Waterbed Effect: Conservation of Sensitivity Dirt



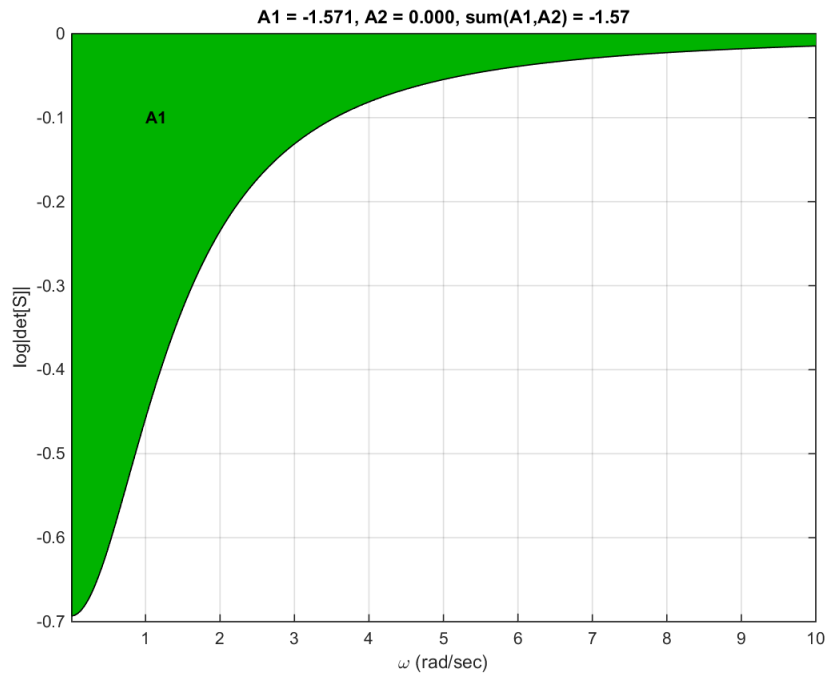
- The Waterbed Effect can be viewed as a “sensitivity dirt,” **conservation** law for control systems.

*Gunter Stein, “Respect the Unstable”, IEEE Control Systems Magazine, Aug. 2003.*

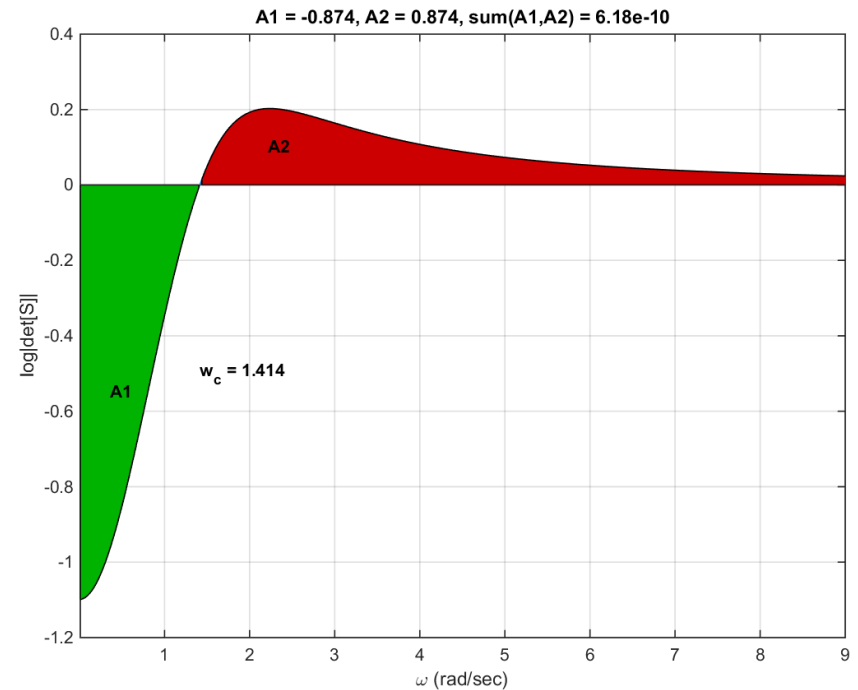


# The Waterbed Effect: Examples

$$L(s) = \frac{1}{(s + 1)}$$

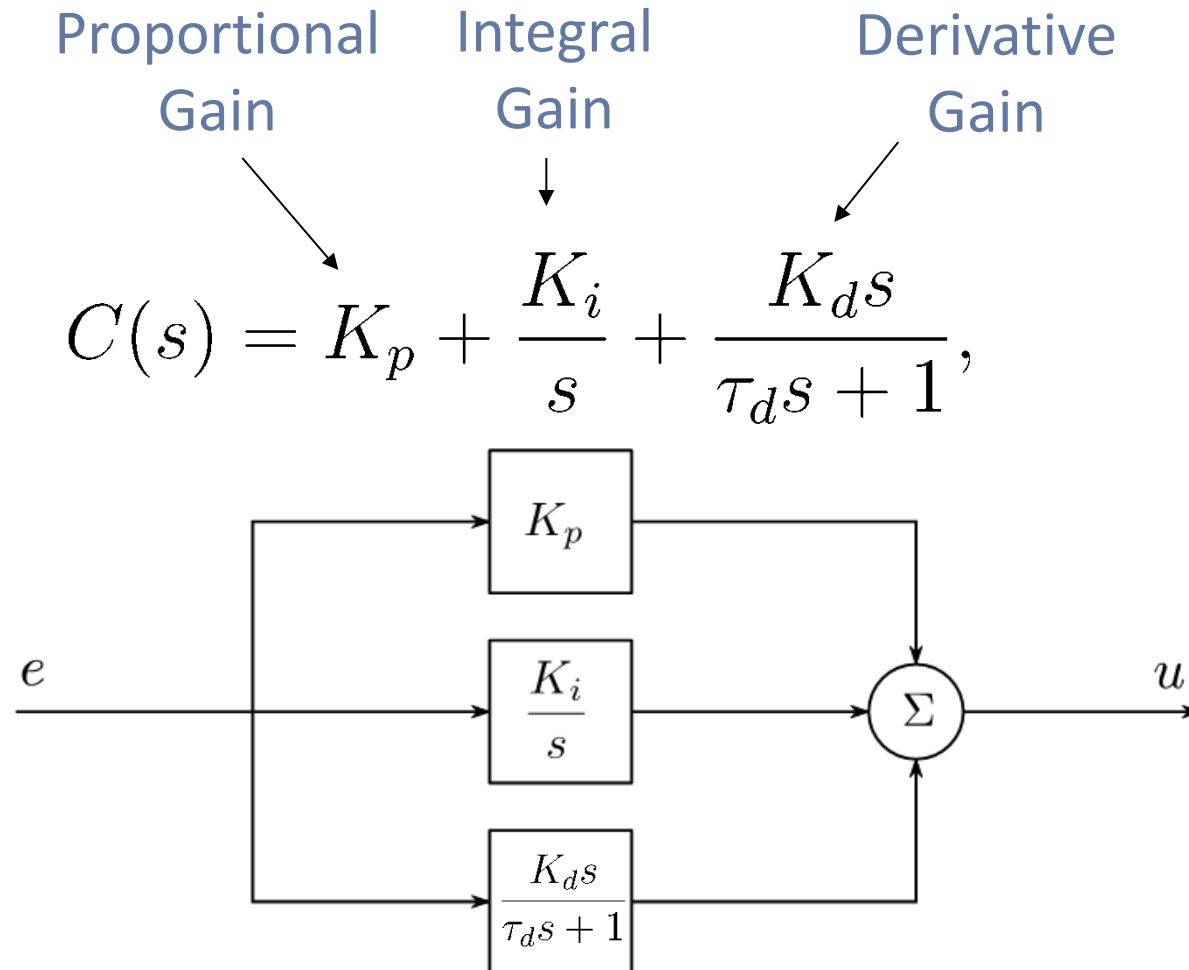


$$L(s) = \frac{2}{(s + 1)^2}$$



- ❑ The Waterbed Effect Theory
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# PID Control Structure



G. F. Franklin, J. D. Powell, and A. Emami-Naeini, *Feedback Control of Dynamic Systems*, 7th ed. Prentice-Hall, 2015.



# PID Tuning Procedure

- Assume the plant can be approximated by:

$$P(s) = \frac{K}{(\tau_1 s + 1)(\tau_2 s + 1)}$$

- Assume the desired closed-loop transfer function is given by:

$$T_{des}(s) = \frac{\omega_{des}^2}{(s^2 + 2\beta\omega_{des}s + \omega_{des}^2)}$$

- Then the following selection of PID tuning parameters will yield the desired closed loop:

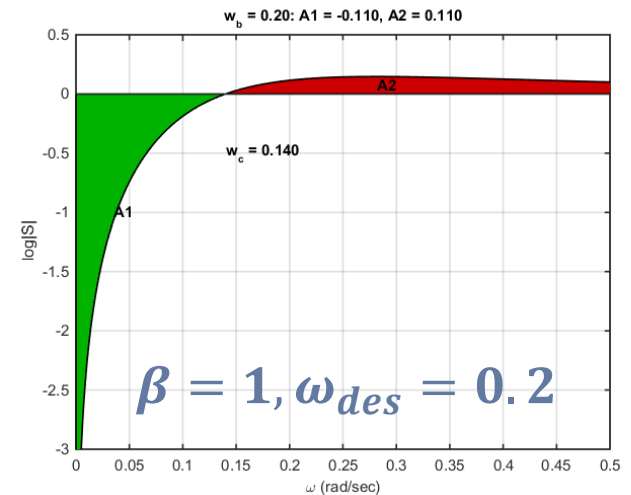
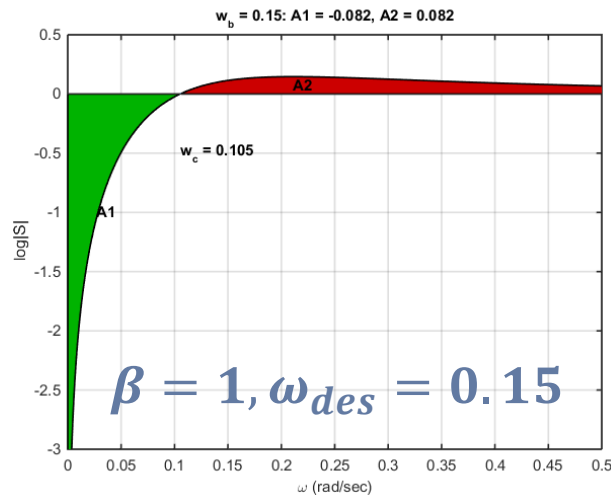
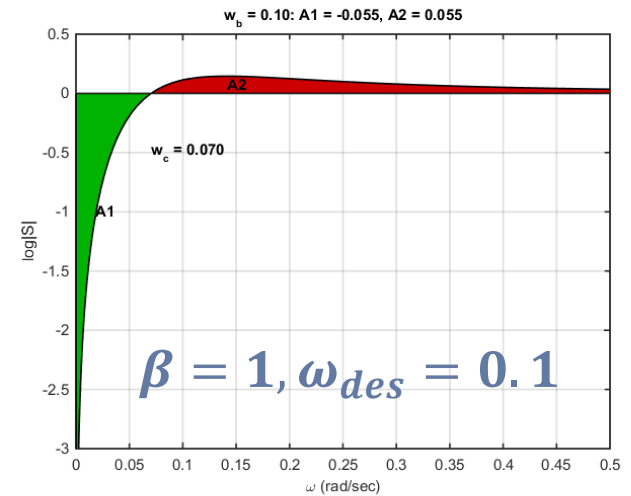
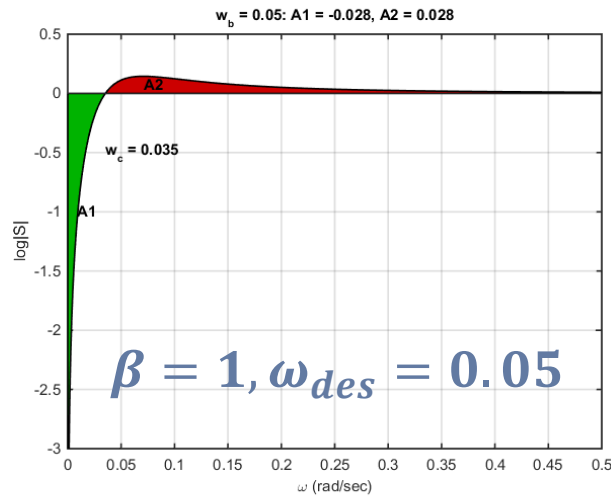
$$K_p = \frac{(2\beta\omega_{des}(\tau_1 + \tau_2) - 1)}{4K\beta^2}, \quad K_i = \frac{\omega_{des}}{2K\beta}$$

$$K_d = \frac{(2\beta\omega_{des}\tau_1 - 1)(2\beta\omega_{des}\tau_2 - 1)}{8K\beta^3\omega_{des}}, \quad \tau_d = \frac{1}{2\beta\omega_{des}}$$

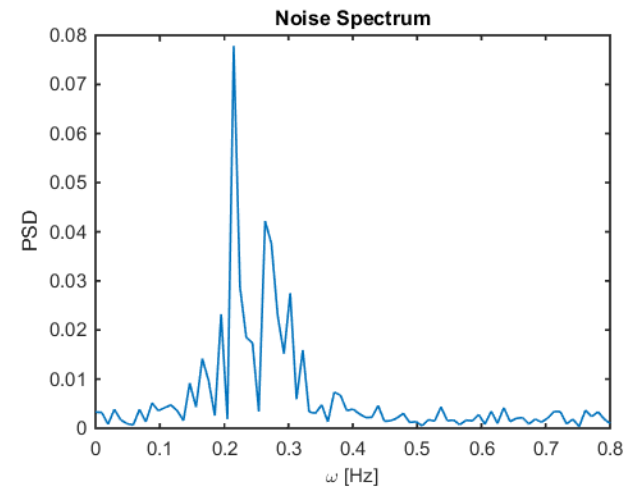
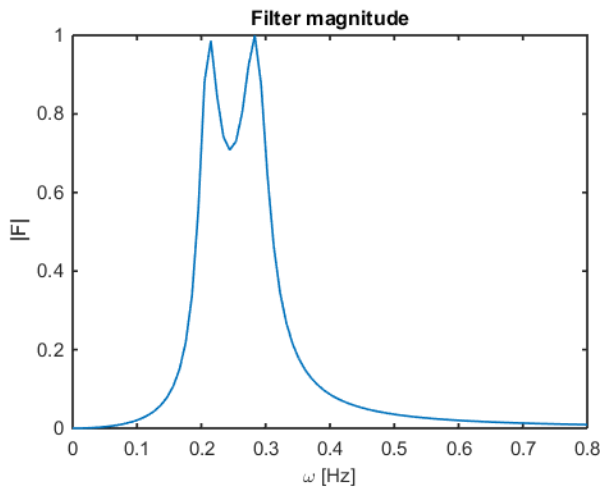
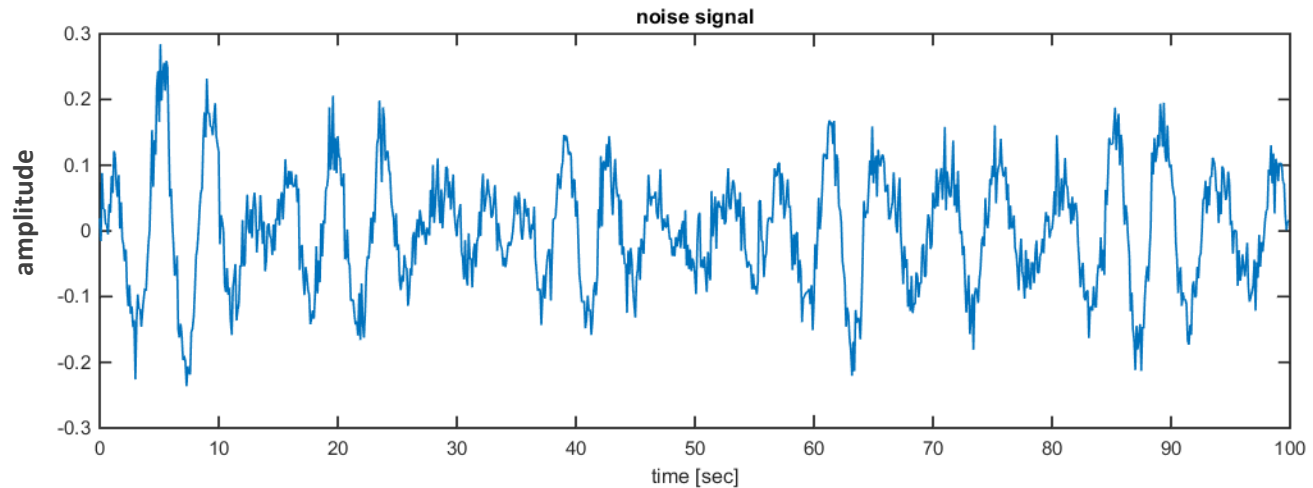
Only 2 tuning knobs:  $\beta$  and  $\omega_{des}$ ! (desired closed-loop **damping** and **bandwidth**)

# Sensitivity Function Tuning

Varying the tuning parameters and inspecting the Waterbed Effect allows for efficient tuning of the desired closed-loop



# Example Noise Signal



The Sensitivity  
Area A2  
amplifies the  
noise spectrum

- ❑ The Waterbed Effect Theory
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# Temperature Control of Heated Plates

- ❑ Temperature control of heated plates is important in many thermal processing systems (RTP, Etch, Bake, MOCVD, etc.)
- ❑ The dynamic response of the system can change considerably depending on operating temperature, wafer types, and/or process conditions
- ❑ Ideally one would like to get the exact same closed-loop temperature response (*performance*) despite these system variations (*robustness*)
- ❑ In this example we will look how changes in system parameters affect the closed-loop dynamics in terms of the waterbed effect

# Thermal Model of Heated Plate

- ❑ A tungsten-halogen lamp is shown heating a plate from below
- ❑ The plate radiates, conducts, and convects heat to the walls and surroundings
- ❑ The system can be divided into a number of control volumes and the heat equation can be written for the net rate of temperature change:

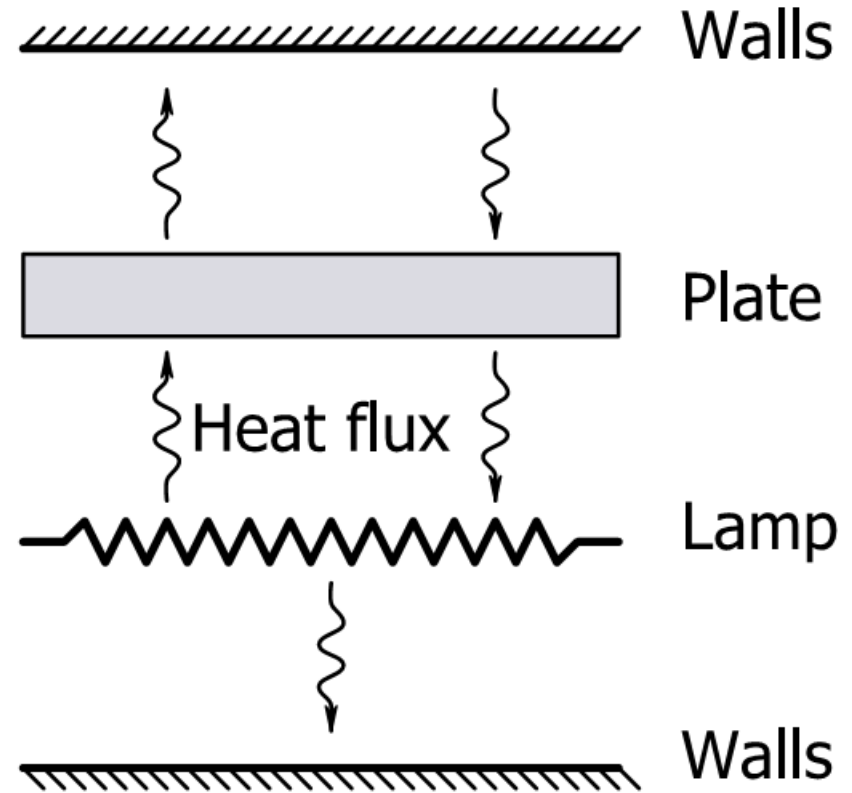
$$\dot{T} = f(T, u), \quad y = g(T),$$

Dynamic System of Equations      Sensed Temperature

For each control volume,  $i$

$$m_i(T) \dot{T}_i = Q_i^r(T) + Q_i^c(T) + Q_i^v(T) + b_i u,$$

Thermal mass      Radiation      Conduction      Convection      Electrical Power In



# Plate Heat Loss – 1D Example

- ❑ The heat loss from the plate to the surroundings

$$q_s = \epsilon \sigma (T_s^4 - T_\infty^4) + h(T_s - T_\infty),$$

Effective emissivity

Effective heat transfer coefficient

Effective emissivity for  
infinite parallel surfaces

$$\epsilon = \frac{1}{\frac{1}{\epsilon_1} + \frac{1}{\epsilon_2} - 1}.$$

Surface 1

Surface 2

We will look at control performance when these two parameters ( $\epsilon$  and  $h$ ) vary.

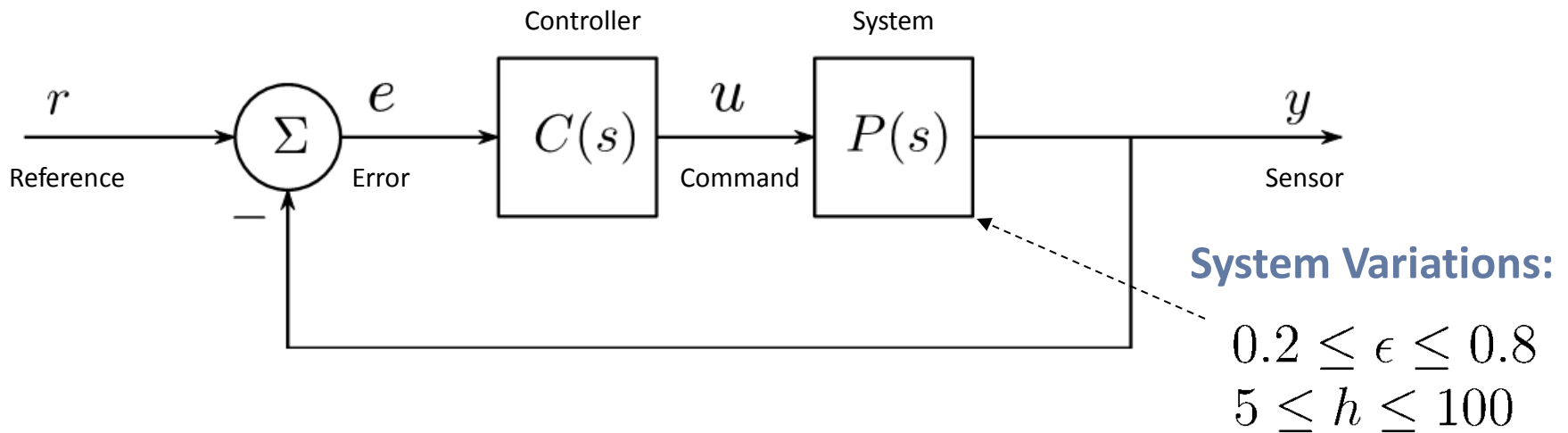
# Process Variations and Robust Control

- ❑ Plate emissivity can change in ways that are difficult to predict
- ❑ Changes in gas flows or gas chemistry can change the heat losses
- ❑ Changes can be “wafer-to-wafer” or during processing (dynamic)
- ❑ If you knew how the losses changed, you could tune the controller for a specific process condition
- ❑ But often you cannot know about changes so the controller must be robust
- ❑ Robustness here is defined as good performance for a wide range of process conditions



# Process Variations and Closed-Loop Control

- Consider the following closed-loop system, where P denotes the heated plate, and C denotes the PID feedback controller



**Heat loss from plate to surroundings:**

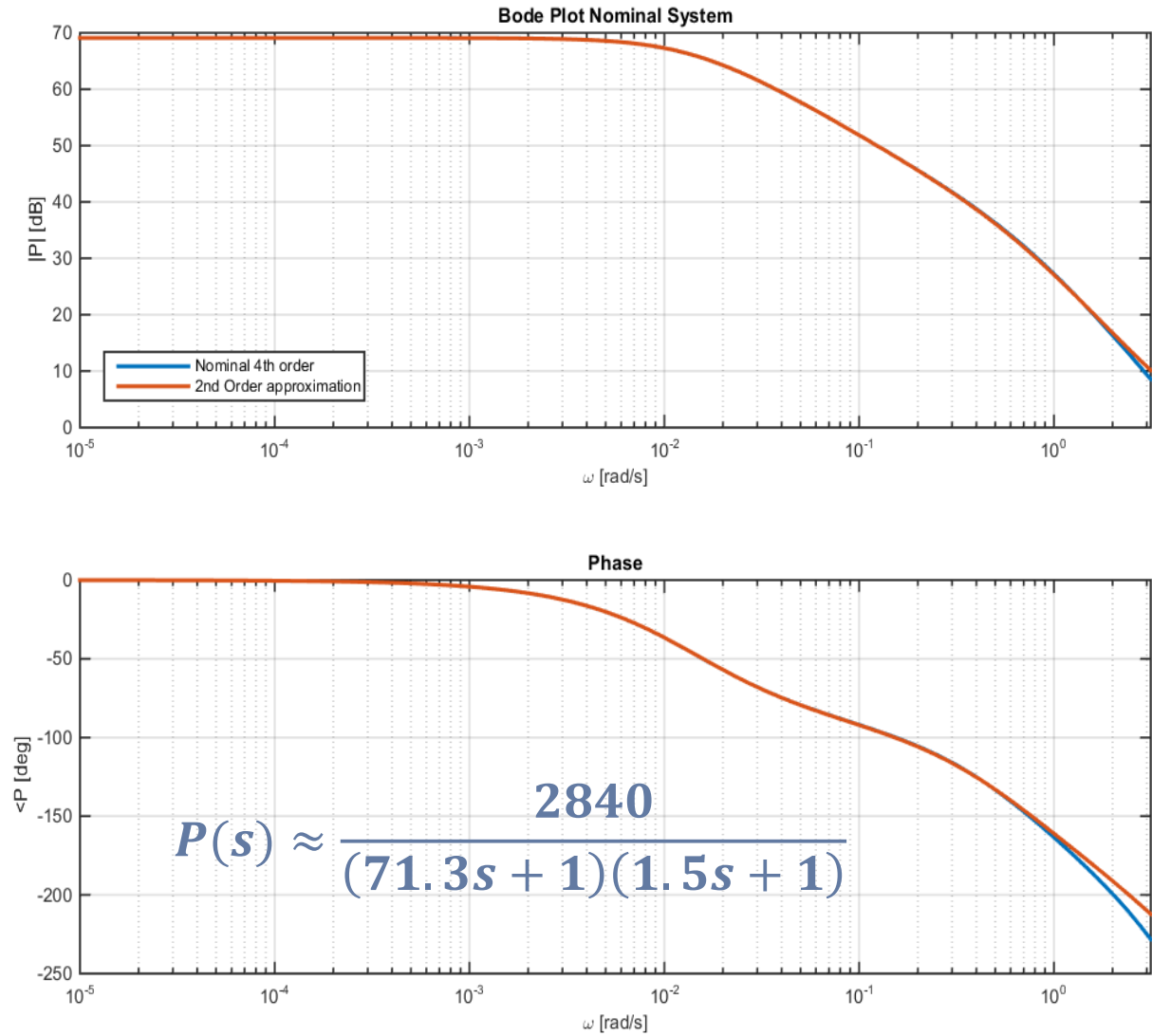
$$q_s = \epsilon \sigma (T_s^4 - T_\infty^4) + h(T_s - T_\infty),$$

Effective  
emissivity

Effective heat  
transfer coefficient

# Bode Plot of Nominal Plant

- Nominal plant is obtained by linearizing non-linear thermal system at operating point  $e_0 = 0.6$ ,  $h_0 = 50$ , and  $T_0 = 600\text{C}$
- Nominal plant can be well approximated by 2<sup>nd</sup> order system



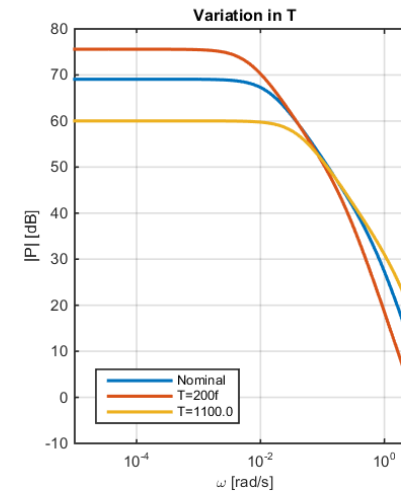
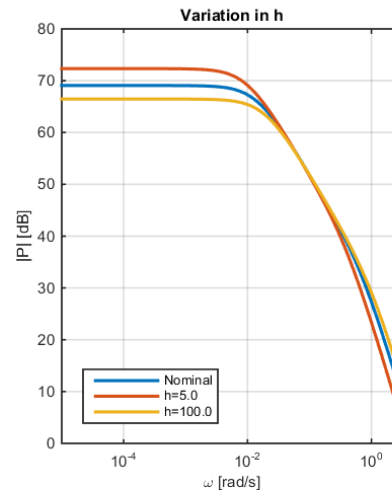
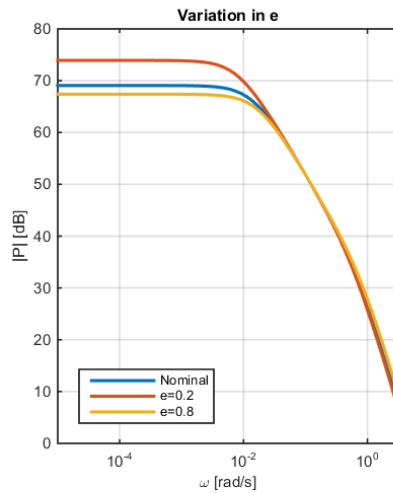
# Bode Plots for Varying System Conditions

## Variation in $e$

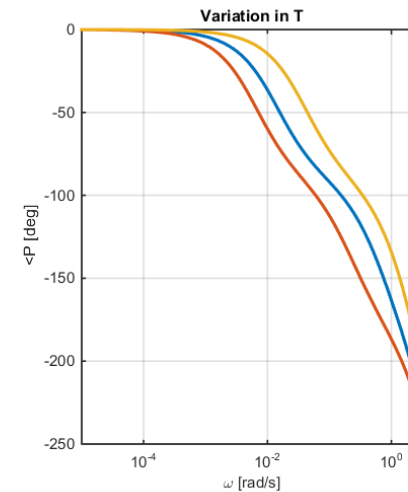
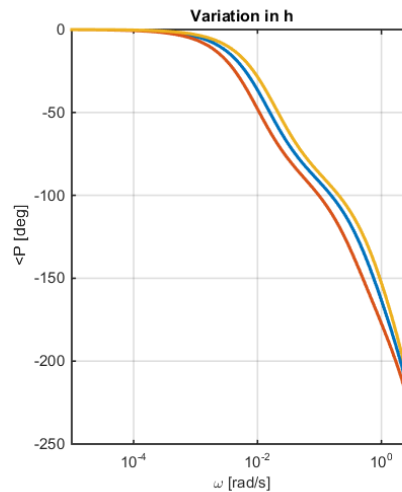
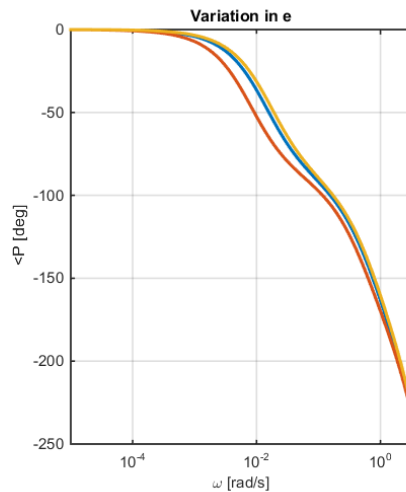
## Variation in $h$

## Variation in $T$

Magnitude



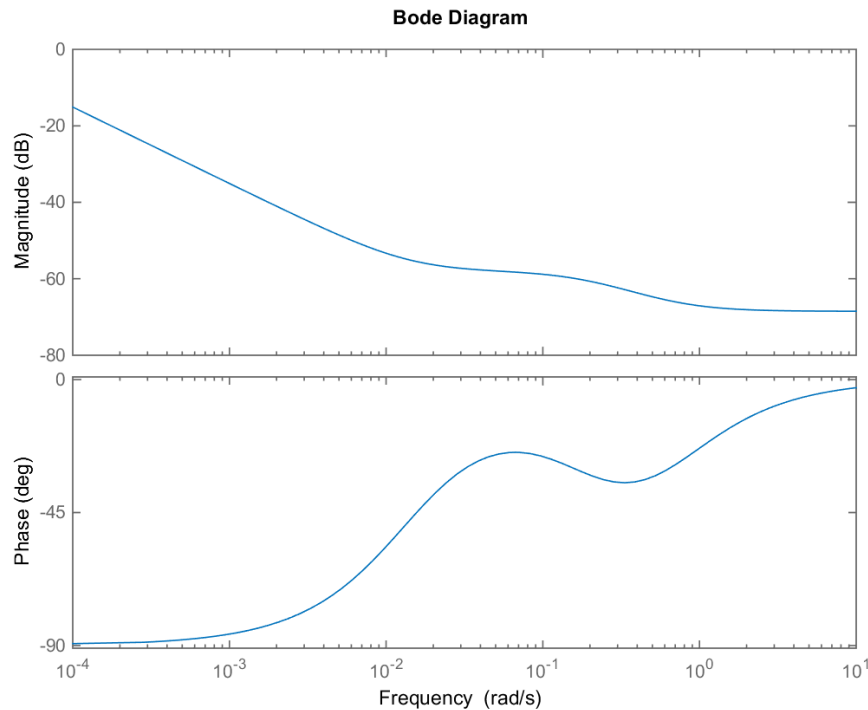
Phase



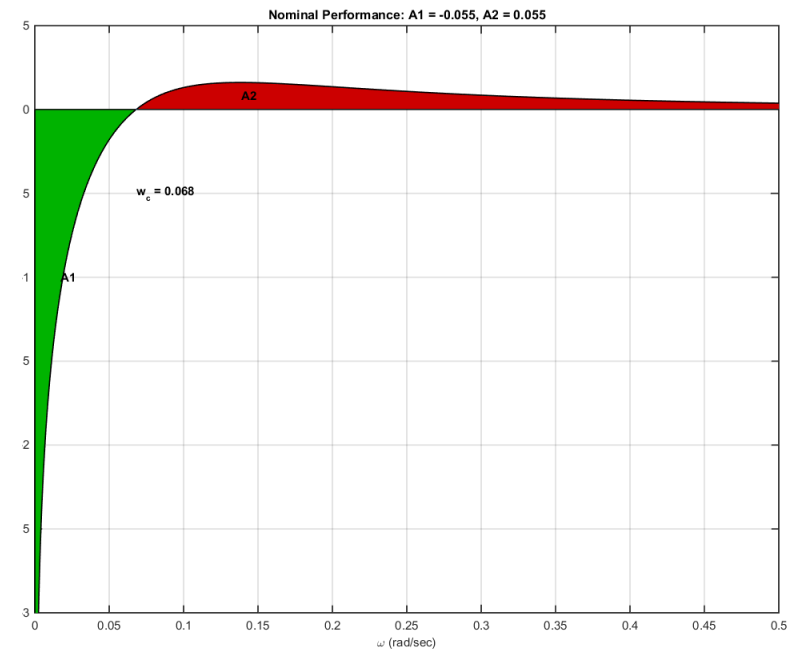
# Control Design for Nominal Plant

- Using the presented PID tuning procedure, a controller was obtained based on the 2<sup>nd</sup> order plant parameters from the previous slide, and tuning parameters  $\beta = 1$ ,  $\omega_{des} = 0.1$  [rad/s]

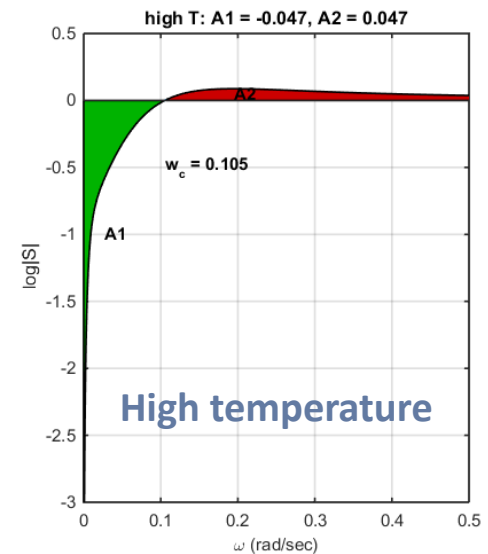
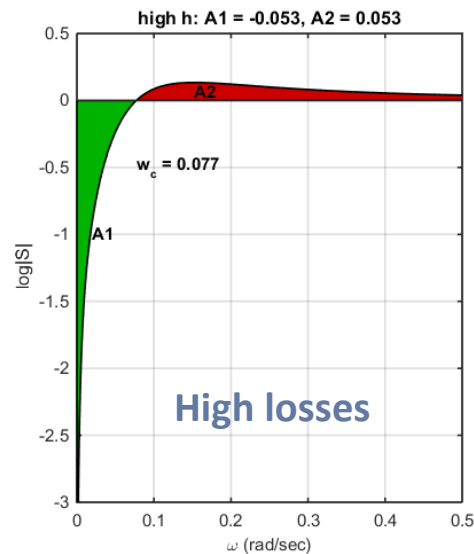
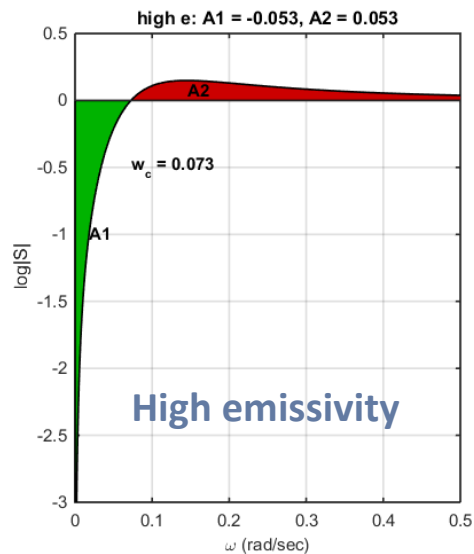
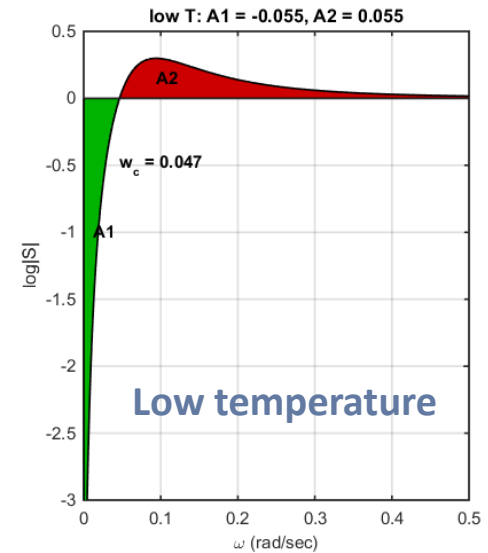
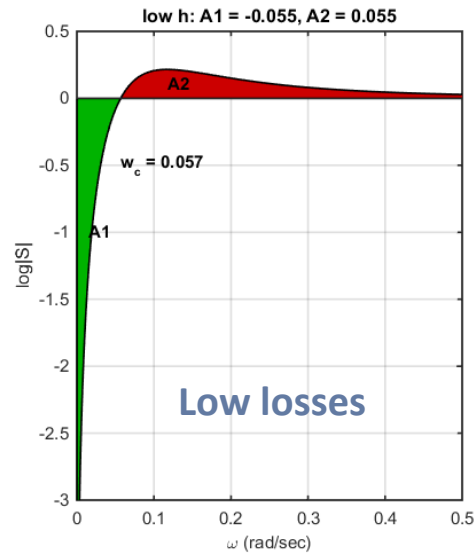
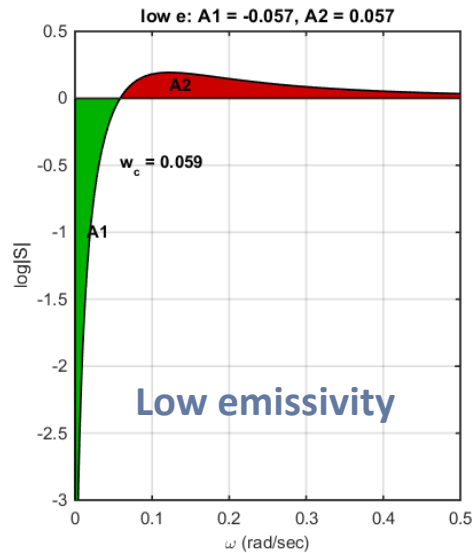
## Bode Plot of PID Controller



## Corresponding Sensitivity Function



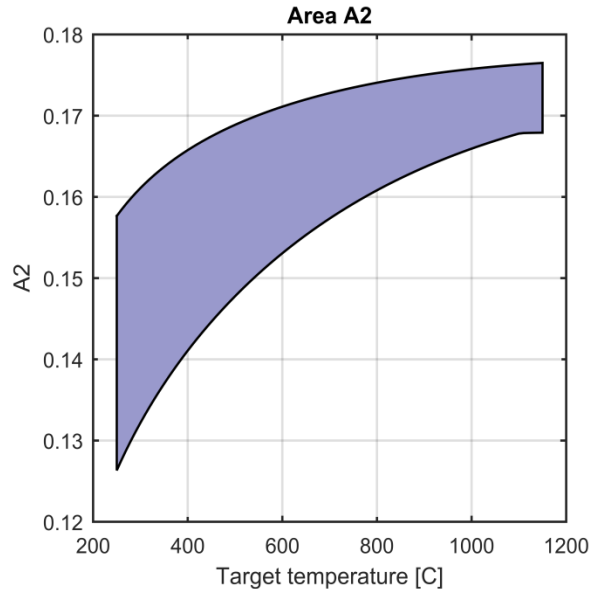
# Sensitivity Functions for Varying Process Conditions



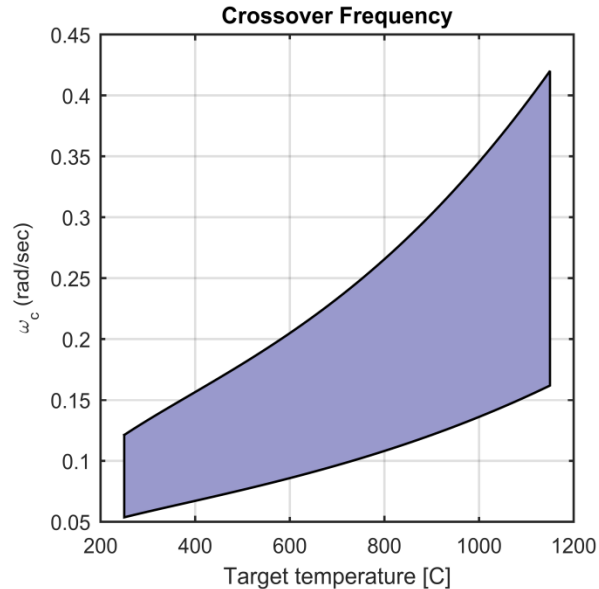
# Waterbed Parameters for Varying Process Conditions

Critical 'waterbed' characteristics of a nominal set of PID parameters for a range of plate properties and operating conditions of a heated plate.

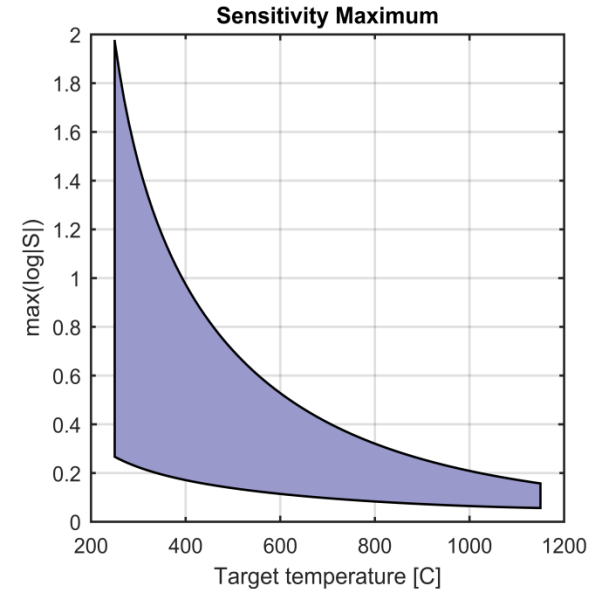
Area A2



Crossover  $\omega_c$



$\max|S|$



- ❑ Summary of 3000 simulations where three critical waterbed parameters were calculated for variations in emissivity and heat transfer coefficient over the entire operating range from 250°C to 1150°C
- ❑ As the target temperature increases, the area for disturbance rejection and corresponding cross-over frequency increases, but so does the area for noise amplification

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# Summary & Conclusions

- ❑ PID controllers are ubiquitous in semiconductor process control
- ❑ We proposed a new method of tuning PID controllers using the fundamental waterbed effect from control systems theory
- ❑ We applied the new methodology to heating of a plate used in semiconductor process control
- ❑ Use of the waterbed effect allows for efficient tuning of PID controllers